

Full-wave simulation of focusing light through scattering layers using the T-matrix method

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We present a physically realistic and efficient method of

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- Background + Motivations 1. Physics of light propagation and *in vivo* implications

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 Wavefront shaping principle and applications

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- 2. Our Contributions + Solutions
 - 1. Constructing our model
 - 1. The discrete particle model of scattering media
 - 2. The T-matrix method theory and peculiarities
 - 3. Simulating wavefront shaping

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 - 1. Numerical validation (Mie theory + finite-difference time-domain)
 - 2. Domain validation (Inverse adding-doubling)

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 - 1. Optimising a focus
 - 2. Enhancement vs elements

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- 3. Conclusions + acknowledgements



Why make a model of WFS?



Why make a model of WFS? What is WFS?



Why make a model of WFS? What is WFS?

• Understanding the

need to model WFS =

understanding

the need for WFS.

Understanding light-tissue interactions

• Understanding the

need to model WFS =

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the need for WFS.

 Many modalities rely on the propagation of visible light through biological tissue.





Jacques, Steven L., Physics in Medicine & Biology, 2013



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Tissue is a strong scatterer



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Highly inhomogeneous refractive index = highly scattering medium

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Gigan, Sylvain., Nature Photonics, 2017

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What is wavefront shaping?



What is wavefront shaping?

Spatially modulating light to construct arbitrary fields



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Optical foci have been generated through very deep domains



Shen, Yuecheng, et al., Journal of biomedical optics, 2016

Optical foci have been generated through very deep domains



Shen, Yuecheng, et al., Journal of biomedical optics, 2016

This is how WFS may increase the depth and resolution of optical imaging.



Horstmeyer, R., et al., Nature Photonics, 2015

Experimental concerns and constraints

Let's consider an experiment shaping light inside scattering media

Modulation methods?

- Phase or amplitude
- SLM or DMD
- Number of elements
- Experimental design

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Domain considerations?

- Phantom design
- Validation
- Controlling decorrelation

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- Feedback limitations?
- Feedback required
- No internal fields
- Limited FOV
- Measuring phase

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- . Measure field inside the medium
 - no feedback mechanism to see inside medium

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Advantages of computational methods

- I. Measure field inside the medium
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- 2. Measure amplitude and phase anywhere
 - full understanding of *in vivo* propagation

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Computational methods are useful to

investigate wavefront shaping

Full-wave modelling of WFS

- Directly solve equations governing light propagation.
- Subwavelength discretization = very computationally expensive.











Dedo, Maxime Irene, et al., Applied Sciences, 2019 Yang, Jiamiao, et al., Optica, 2019





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Efficient, full-wave, computational methods

are useful to investigate wavefront shaping



We present a physically realistic and efficient method of

modelling wavefront shaping (WFS) through scattering media.



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1. Constructing our model – how do we simulate WFS?



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We present a physically realistic and efficient method of modelling wavefront shaping (WFS) through scattering media.

- **1.** Constructing our model how do we simulate WFS?
- **2.** Validating our model *is our model accurate?*
- **3.** Focusing through titanium dioxide phantoms can we simulate WFS?
- **4.** Exploiting our model what is special about our model?



Constructing our model: The discrete particle model of scattering media

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Jacques, Steven L., Physics in Medicine & Biology, 2013

Constructing our model: The discrete particle model of scattering media







Simulating discrete particle domains

•



T-matrix is an extension of Mie theory to multi-sphere domains

• Total field is the sum of the scattered fields from each individual sphere.



Simulating discrete particle domains





• Total field is the sum of the scattered fields from each individual sphere.





Scaling of the T-matrix method

Simulating discrete particle domains





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Scaling of the T-matrix method







Our method for simulating WFS

1. Use Mie theory to design discrete particle domain.





- 1. Use Mie theory to design discrete particle domain.
- 2. Use the T-matrix method to simulate the propagation of light through said domain.



- 1. Use Mie theory to design discrete particle domain.
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- 3. Generate new input mode by simulating propagation from a difference incident angle. [mm] z [µm] (μm) 50 -50 Scattering medium 2nd input mode 1st input mode *not to scale

- 1. Use Mie theory to design discrete particle domain.
- 2. Use the T-matrix method to simulate the propagation of light through said domain.
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- 4. Modulate these input modes to shape light through the medium

Our method for simulating WFS

- Use Mie theory to design discrete particle domain. 1.
- Use the T-matrix method to simulate the propagation 2. of light through said domain.
- Generate new input mode by 3. simulating propagation from a difference incident angle.
- Modulate these 4. input modes to shape light [mm] through the medium [µm] z [µm] -50 Scattering medium 2nd input mode 1st input mode *not to scale

Constructing a titanium dioxide domain



Vellekoop and Mosk, Optics letters, 2007

Consider replicating Vellekoop and Mosk

- 1. Use Mie theory to design discrete particle domain.
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- Consider replicating Vellekoop and Mosk
- Use Mie theory to generate a highly scattering TiO₂ phantom (transport mean free path of ~5µm⁻¹).

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- Simulate propagation of plane waves incident at various angles (-10-10° polar and azimuthal).

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- Simulate propagation of plane waves incident at various angles (-10-10° polar and azimuthal).
- Stepwise sequential algorithm used to spatially modulate light.



Validating the model

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Numerical validation (*Mie theory* + *FDTD*)



• Compared single sphere fields against Mie theory to validate numerical implementation of T-matrix.



Validating the model



• Compared single sphere fields against Mie theory to validate numerical implementation of T-matrix.



Domain validation (Inverse Adding-Doubling) Total field Scattered field IAD can be used to independently Transmittance measure the optical properties of a domain. 0 x [μm] x [μm] Reflectance Sphere aperture Beam 0 x [μm] 0 x [μm]

Measurements of transmittance and reflectance were taken by simulating the propagation of a Gaussian beam through scattering domains. For all domains, IAD derived scattering coefficients and anisotropies matched theory (<3% error).



Focusing through titanium dioxide phantoms

Using iterative phase modulation to focus through TiO₂ (can we model WFS?)



Focusing through titanium dioxide phantoms

Using iterative phase modulation to focus through TiO₂ (can we model WFS?)



Vellekoop and Mosk, Optics letters, 2007

Replicating original Vellekoop and Mosk demonstration by focusing through TiO₂



Focusing through titanium dioxide phantoms

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Using iterative phase modulation to focus through TiO₂ (can we model WFS?)





Using iterative phase modulation to focus through TiO₂ (can we model WFS?)









Our method is capable of generating arbitrary fields, as shown above



3D & internal focusing

- Computational models can be used to evaluate the field at arbitrary locations.
- Below is a 3D focus optimized to generate inside the TiO₂ domain.



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Measuring the angular 10 memory effect range

Ansatz methods have struggled to model coherent phenomena (e.g. memory correlations)

Some methods exploit these correlations to focus light into scattering media.

-10

-10



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Modelling the angular range of an optimized focus

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Imaging FOV could be increased by exploiting memory correlations to translate already optimized foci.

Focusing might also be able to be accelerated by exploiting priors (e.g. sharing phase maps between input modes).



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Enhancement vs focus size



a 0.0 b 0.0 b 0.0 b 0.5 b 0.4 b 0.5 b 0.4 c 0.2 c 0.1 c 0.0 c

Relationship between enhancement and focus size important for photoacoustic wavefront shaping

Modelling the angular range of an optimized focus

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15

10

5

0

-5

-10

-15

-60

x [Jm]

1. WFS has the potential to enhance the depth and resolution of optical imaging modalities.

-20

0

z [µm]

-40



15

10

5

0

-5

-10

-15

-60

x [μm]

- 1. WFS has the potential to enhance the depth and resolution of optical imaging modalities.
- 2. Computational models can augment research of WFS by allowing for the measurement of internal fields and phase.

-20

0

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15

10

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x [hm]

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- 3. We have presented and validated a physically realistic yet computationally efficient model of WFS. The model has replicated existing WFS research and is being exploited to investigate the shaping of light into biological tissue.

-20

0

z [µm]



15

10

5

0

-10

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[mm]

× ₋₅

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If interested, please attend my P+U talk tomorrow.

-20

0

z [µm]



Acknowledgements

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ROYAL

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National Institute for Health Research



Contact details